Equation (2.3) on page 38 defines the ISBN by a weighted sum where digit $d_{i}$ is multiplied by $11-i$. It is more elegant to multiply $d_{i}$ by $i$ and write the ISBN in the form

$$
\begin{equation*}
\mathrm{ISBN}=11-\left(\sum_{i=1}^{9} i d_{i}\right) \bmod 11 \tag{2.3a}
\end{equation*}
$$

To see why equations (2.3) and (2.3a) are arithmetically identical, we look at a representative digit such as $d_{2}$. In Equation (2.3) this digit is multiplied by 9 and those familiar with modulo computations know that $9 d_{2} \bmod 11=2 d_{2} \bmod 11$. Those who demand a proof can obtain it by first denoting $T=9 d_{2} \bmod 11$ and then observing that

$$
\begin{aligned}
9 d_{2} \bmod 11 & =T \\
\left(9 d_{2}+2 d_{2}\right) \bmod 11 & =T+\left(2 d_{2} \bmod 11\right) \\
11 d_{2} \bmod 11 & =T+\left(2 d_{2} \bmod 11\right) \\
0 & =T+\left(2 d_{2} \bmod 11\right) \\
T & =2 d_{2} \bmod 11 \\
9 d_{2} \bmod 11 & =2 d_{2} \bmod 11 .
\end{aligned}
$$

